

## LA-UR-19-26743

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Title: Verification Study of Metal Additive Manufactured Stretch-Dominated Lattices

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Intended for: Report

Issued: 2019-07-16

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# **Verification Study of Metal Additive Manufactured Stretch-Dominated Lattices**

Brandon J. Bogle, Howard J. Rathbun

April 10, 2019

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# **Outline**

**Stretch-Dominated & MAM**

**Beam Member Modeling**

**Continuum Element Modeling**

**Beam & Continuum Comparison**

**3-Point Beam Bending**

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# **Stretch-Dominated & MAM**

Beam Member Modeling

Continuum Element Modeling

Beam & Continuum Comparison

3-Point Beam Bending

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# Areas of Impact

- Medical
- Aerospace
- Safety
- Sport, and etc.



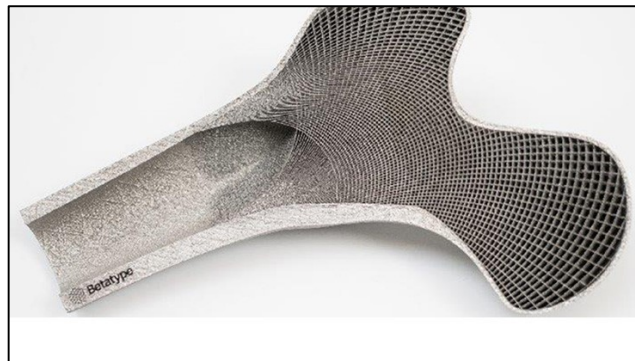
(Engadget, 2019)



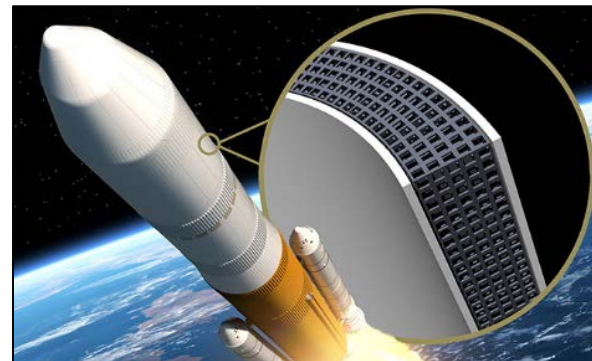
(TCT Mag, 2017)



(3DMPMAG, 2017)



(TMD, 2018)

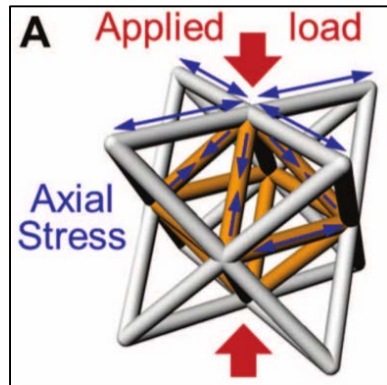


(ETHZ, 2016)

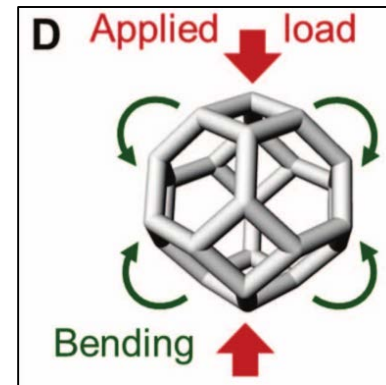
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# Cellular Structures

- Ordered structures are lattices while randomly ordered structures are foams.
- Two classes of lattice structures
  - **Stretch dominated**
  - **Bend dominated**



Stretch Dominated  
(X. Zheng et al, 2014)



Bend Dominated  
(X. Zheng et al, 2014)

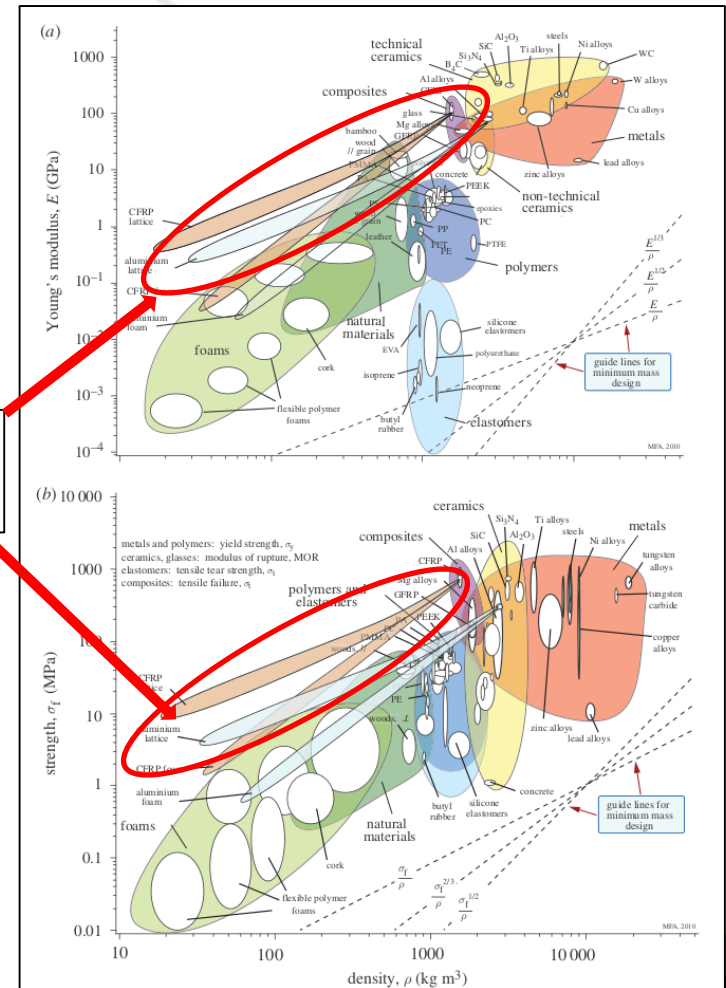
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# Stretch Dominated Properties

- Young's Modulus and yield strength scale linearly with relative density
- Principal Deformation in axial direction (struts)
- Higher yield strength than bend dominated

Cellular Structures

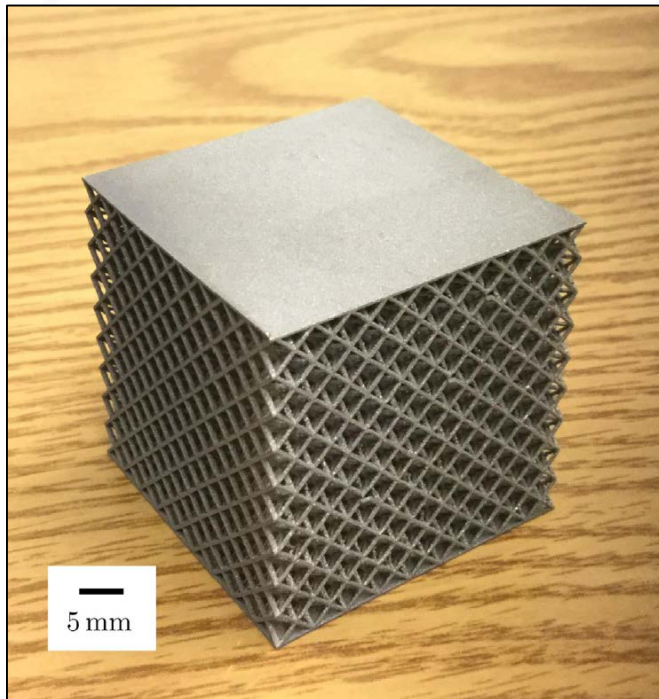


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(N. Fleck et al, 2014)



# Metal Additive Manufacturing



(M. Messner et al, 2015)

- Development has enabled accurate construction of complex 3D structures.
- Control of micro-geometries means properties can be designed based on structure.

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Stretch-Dominated & MAM

## **Beam Member Modeling**

Continuum Element Modeling

Beam & Continuum Comparison

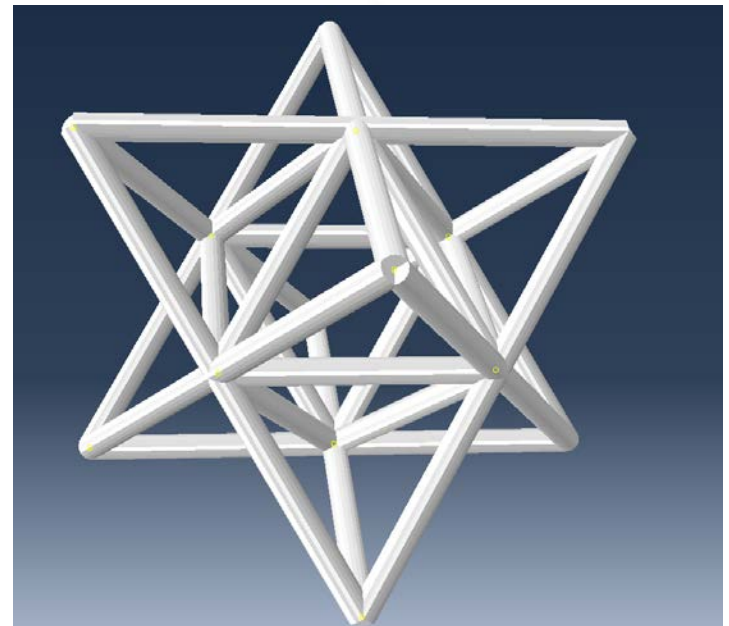
3-Point Beam Bending

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# Beam Element Modeling

- Recreated literature model using beam element in Abaqus
- Octet design conditions:
  - Relative density ( $\bar{\rho}$ ) = 10%
  - Strut length ( $l$ ) = 3 mm

$$\bar{\rho} = 6\sqrt{2}\pi\left(\frac{a}{l}\right)^2$$



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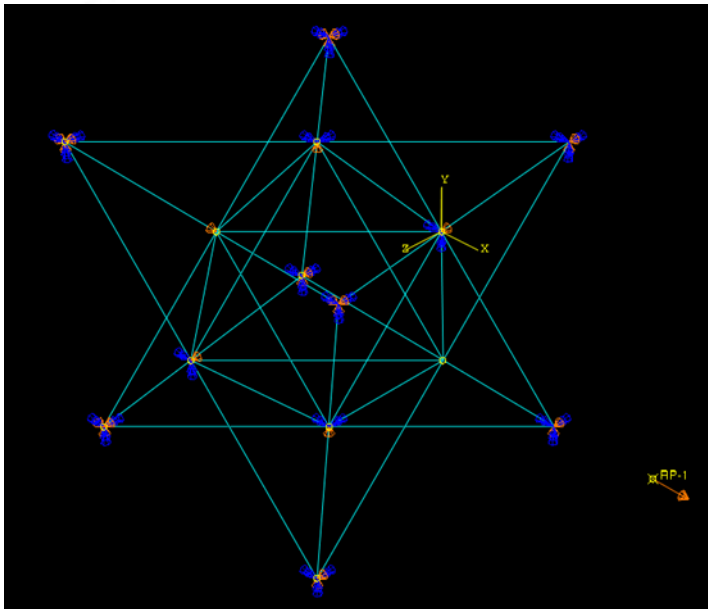
# Beam Element Characteristics

## ■ Material Properties:

<b>Density</b> (tonnes/mm <sup>3</sup> )	1.13e-9
<b>Elastic Modulus</b> (MPa)	1780
<b>Poisson Ratio</b>	0.35
<b>Yield Stress</b> (MPa)	40
<b>Plastic Strain</b>	0

## ■ Boundary conditions

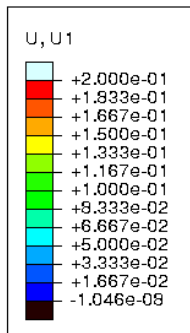
- Displacement in x-direction
- Symmetry boundary in y- and z-directions



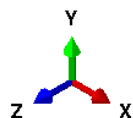
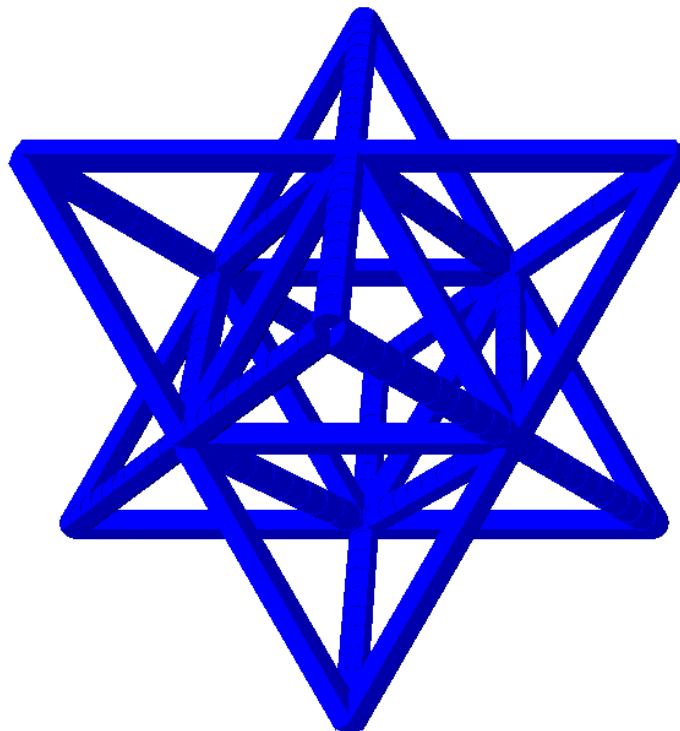
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# Beam Element ODB Video

Step: Displace Frame: 0  
Total Time: 0.000000



**Max Displacement = 0.2 mm**



Displacement in the +X-direction with no symmetry BC  
ODB: X\_DISP\_NoSymBC.odb Abaqus/Standard 3DEXPERIENCE R2019x HotFix 3 Fri Feb 08 16:14:54 MST 2019

Step: Displacement, Displacement in +X-direction  
Increment 0: Step Time = 0.000  
Primary Var: U, U1  
Deformed Var: U Deformation Scale Factor: +4.550e+00

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Stretch-Dominated & MAM

Beam Member Modeling

**Continuum Element Modeling**

Beam & Continuum Comparison

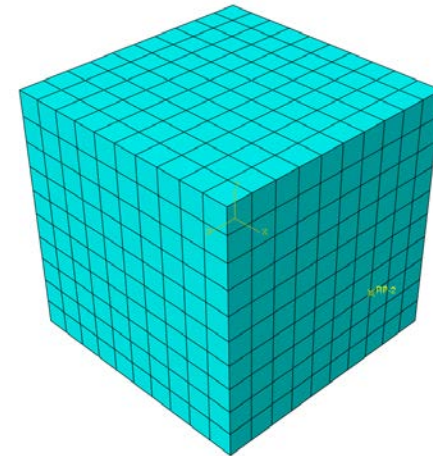
3-Point Beam Bending

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# Continuum Element Modeling

- Use of representative volume elements for unit cell (UC) would decrease total elements
- Same BC's and material properties except for stiffness
  - Set as orthotropic for linear elastic response



$$\begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{23} \\ \sigma_{13} \\ \sigma_{12} \end{bmatrix} = E\bar{\rho} \begin{bmatrix} \frac{1}{6} & \frac{1}{12} & \frac{1}{12} & 0 & 0 & 0 \\ \frac{1}{12} & \frac{1}{6} & \frac{1}{12} & 0 & 0 & 0 \\ \frac{1}{12} & \frac{1}{12} & \frac{1}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{12} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{12} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{12} \end{bmatrix} \begin{bmatrix} \varepsilon_{11} \\ \varepsilon_{22} \\ \varepsilon_{33} \\ 2\varepsilon_{23} \\ 2\varepsilon_{13} \\ 2\varepsilon_{12} \end{bmatrix}$$

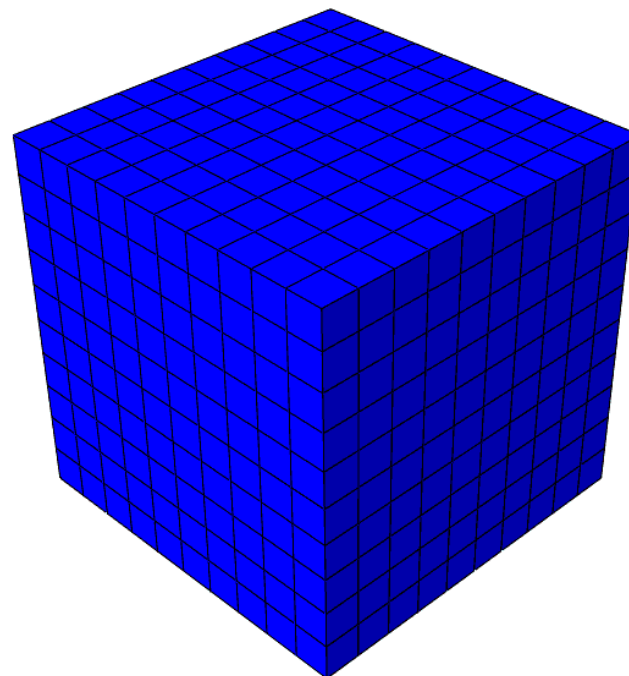
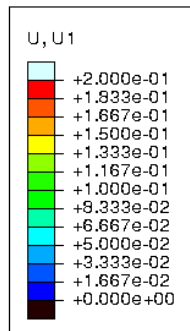
(M. Messner et al, 2015)

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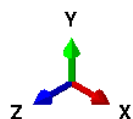


# Continuum Element ODB Video

Step: Displace Frame: 0  
Total Time: 0.000000



**Max Displacement = 0.2 mm**



0.2 mm Displacement in the positive x-direction for small cube

ODB: SmallCube\_Point2mm\_DISP.odb Abaqus/Standard 3DEXPERIENCE R2018x HotFix 3 Wed Mar 20 14:06:52 MDT 2019

Step: Displacement, Displacement in the +x-direction

Increment 0: Step Time = 0.000

Primary Var: U, U1

Deformed Var: U Deformation Scale Factor: +3.000e+00

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Beam Member Modeling

Continuum Element Modeling

**Beam & Continuum Comparison**

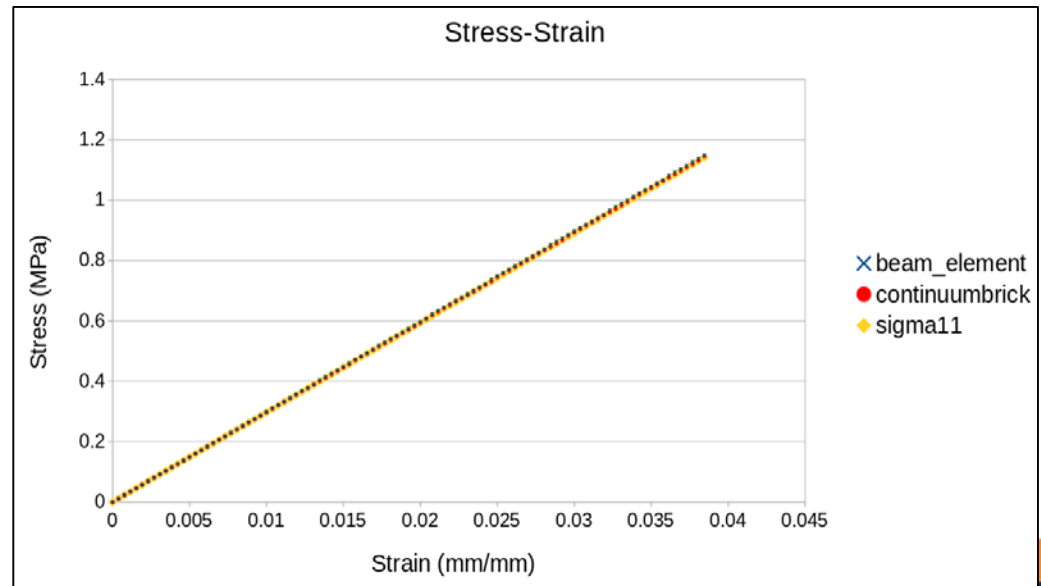
3-Point Beam Bending

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# Comparing Models

- Used reaction force and displacement of reference point for stress-strain curve
- From stiffness matrix, derived analytical solution for stress-strain relationship

$$\sigma_{11} = \frac{E * \bar{\rho} * \epsilon_{11}}{6}$$



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Stretch-Dominated & MAM

Beam Member Modeling

Continuum Element Modeling

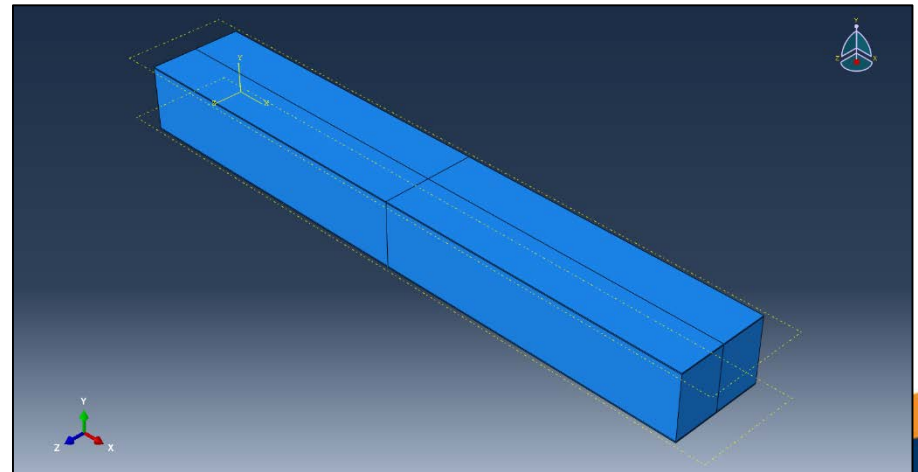
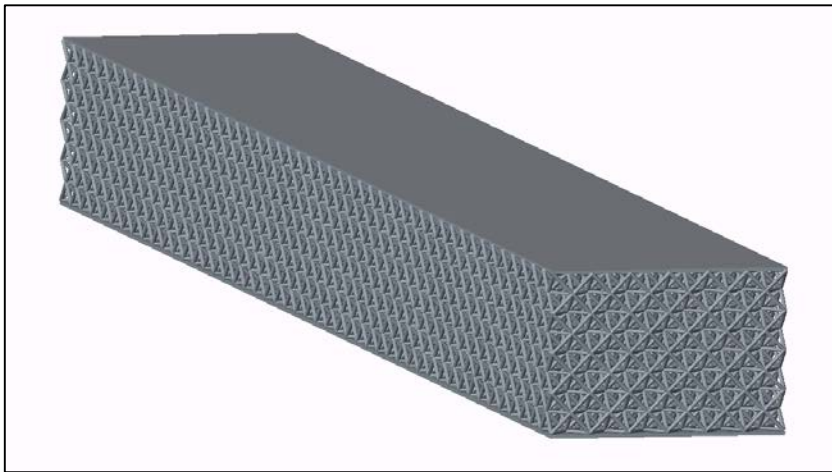
Beam & Continuum Comparison

## **3-Point Beam Bending**

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# 3 Point Bending Test

- Compare model to test data
- Beam consists of octet lattice with face plates
  - Length=47 UC (~200 mm), Width= 6 UC (~25 mm), Height=4 UC (~17 mm)
  - 1128 Unit Cells
- Model with representative volume elements



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# Future Work

- Perform mesh verification study
- Determine bending beam analysis criteria
- Look into other stretch dominated and bend dominated structures
- Compare lattice structures to topology optimization structures.

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# Questions?

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